

Coupled Pendulum

Aim

To study normal modes of oscillations of two coupled pendulums and to measure the frequencies of these normal modes, as well as the spring constant k .

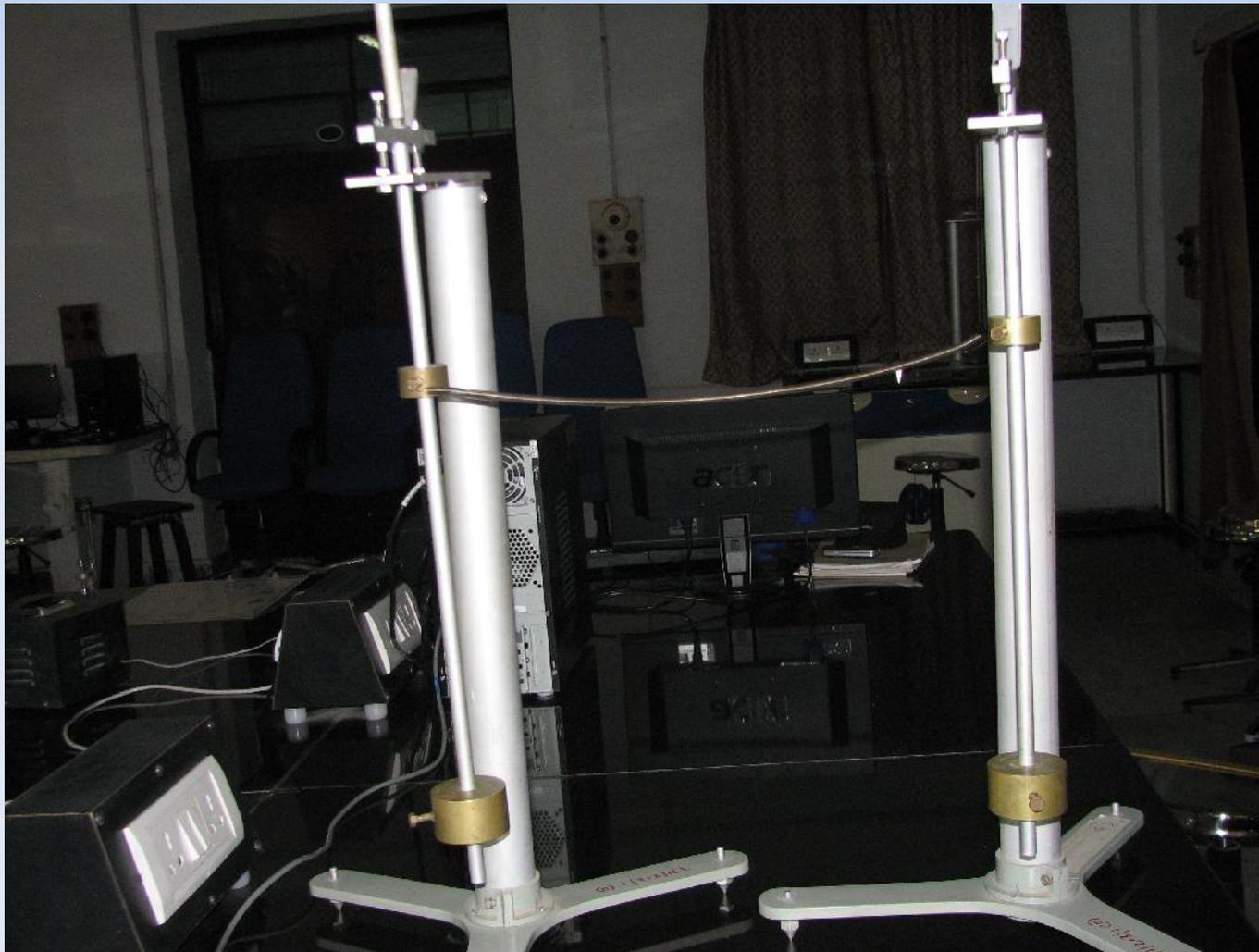
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Apparatus

- **Two compound pendulums**
- **Coupling spring**
- **Stop watch**

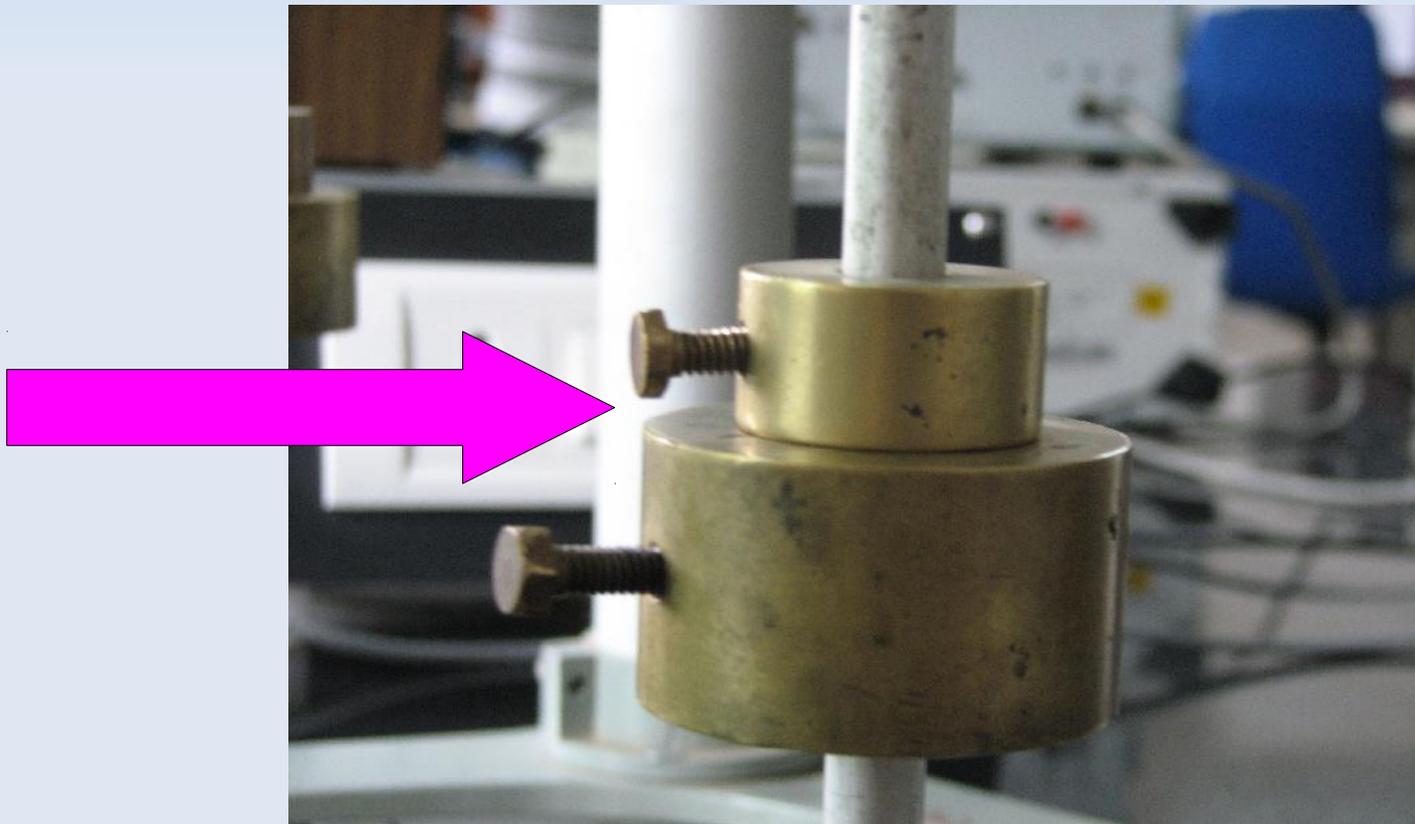
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The Set-up



Procedure (Part I)

- **Uncouple the two pendulums (remove the spring) and bring the peg to which the spring is attached at the bottom.**

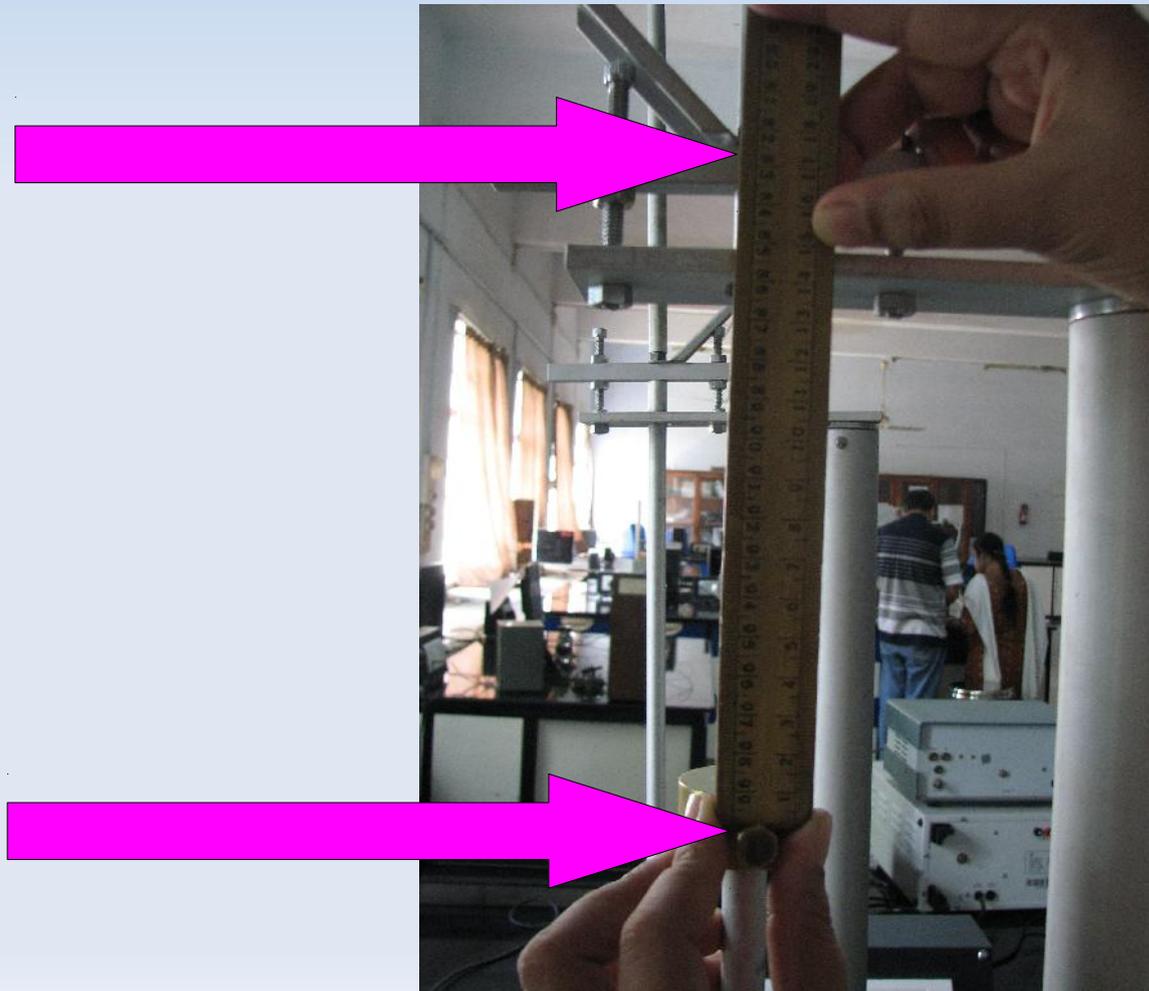


Procedure (Part I)

- **Set small oscillations in both the pendulums individually and measure period T for 20 oscillations. Calculate natural frequency ω_0 .**

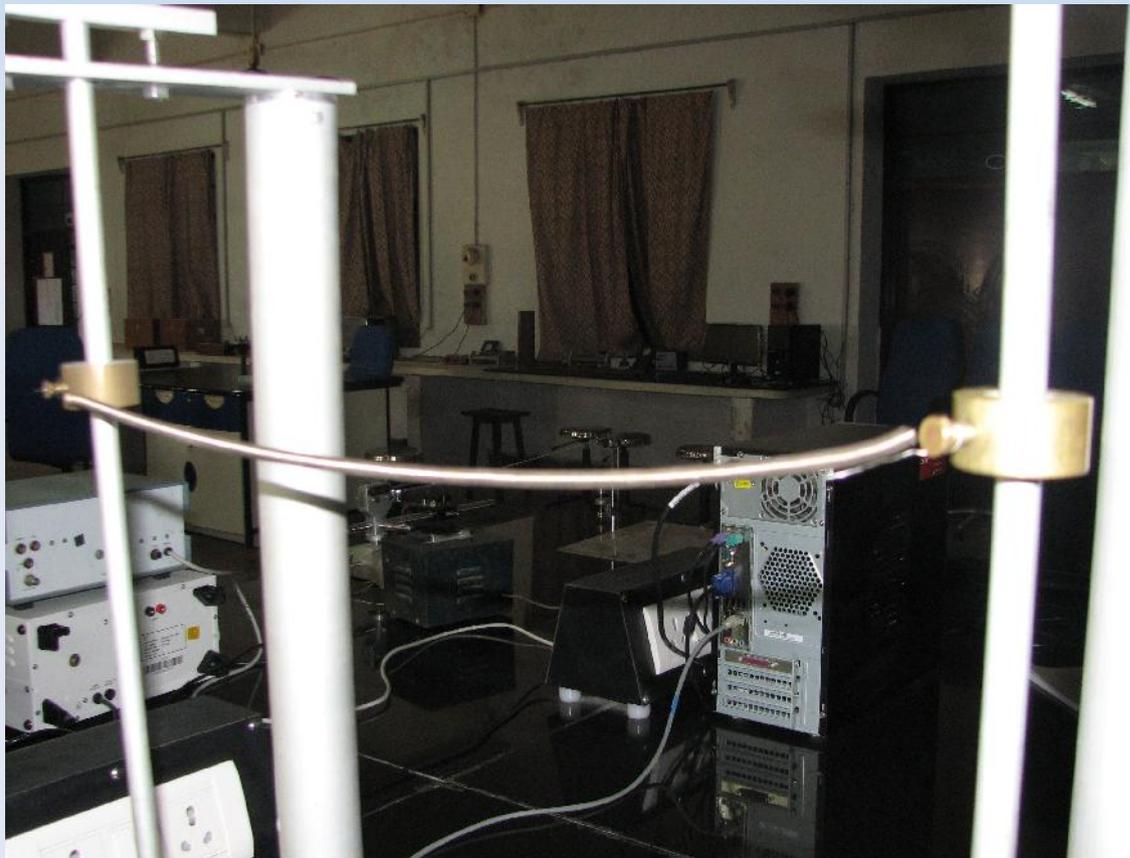
Procedure (Part I)

- The height l (10, 15, and 20 cm) of the peg to which spring is attached is measured from the mid point of the peg to the pivot.



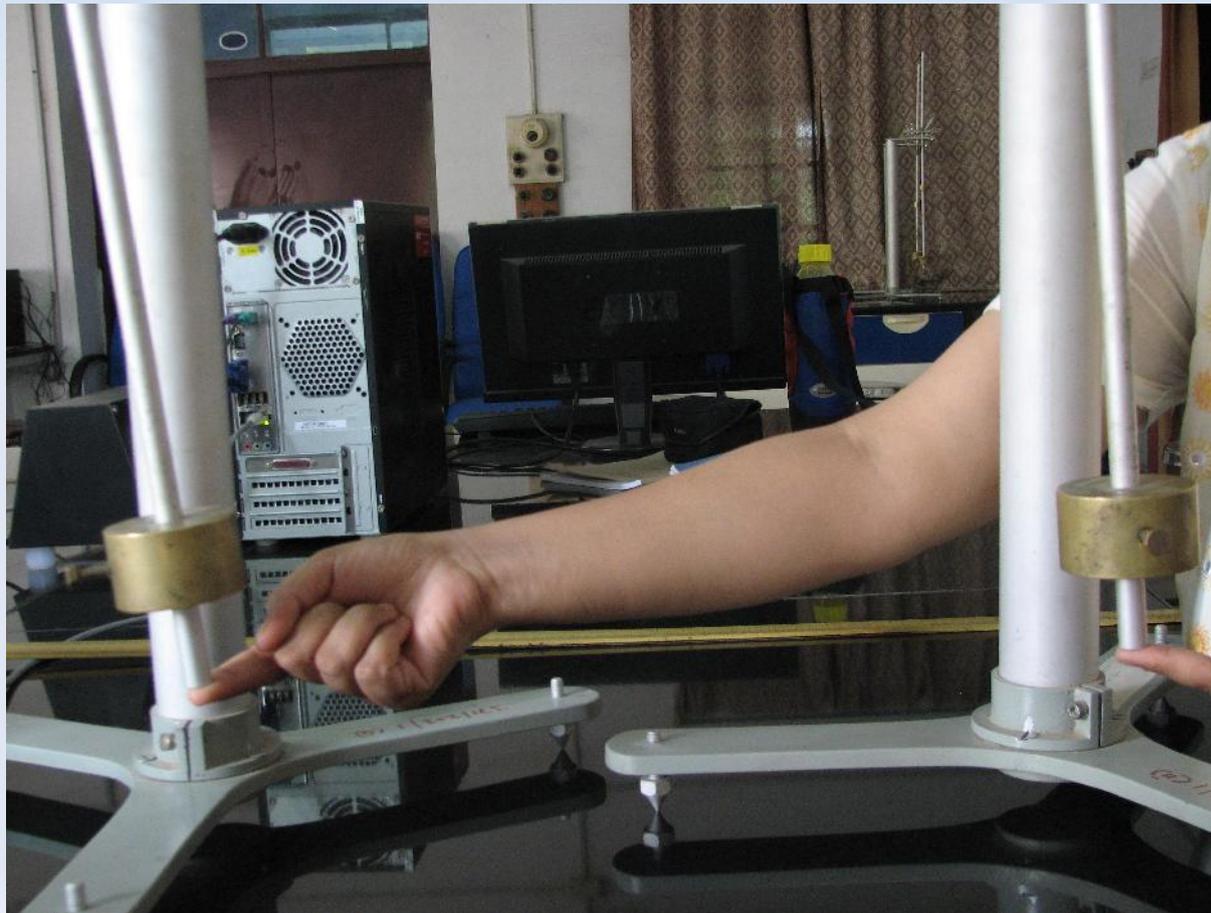
Procedure (Part I)

- Hook the spring at $l=10$ cm. Make sure the spring should neither slack nor stretch.



Procedure (Part I)

- Displace both the pendulums **SLIGHTLY in one direction by the same amount** to excite the in-phase normal mode. Calculate T_1 and ω_1 for 20 oscillations.



Procedure (Part I)

- Now displace both the pendulums **SLIGHTLY in opposite directions by the same amount** to excite the out-of-phase normal mode. Calculate T_2 and ω_2 for 20 oscillations.



Procedure (Part I)

- Repeat the procedure for $l=15$ cm and $l=20$ cm.

Procedure (Part II)

- Set $l=10$ cm.
- Displace any one pendulum by a small amount.
- Measure T for a single (one) oscillation.
(For this, measure T for 20 oscillations and divide the number by 20.)
- Measure time period ΔT between two successive stops of the same pendulum.
- Using these T and ΔT , verify the frequencies, ω_1 and ω_2 , measured in part I.

Calculations and Graphs

- Plot $\frac{\omega_1^2}{\omega_0^2}$ versus l^2 and $\frac{\omega_2^2}{\omega_0^2}$ versus l^2 .
- From the slope of $\frac{\omega_2^2}{\omega_0^2}$ versus l^2 , calculate the spring constant of the coupling spring.

$$\text{Slope} = 2k/mgL$$

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The End